

Digital Chaotic Synchronized Communication System

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Abstract

The experimental study of a secure chaotic synchronized communication system is presented. The synchronization between two digital chaotic oscillators, serving as a transmitter-receiver scheme, is studied. The oscillators exhibit rich chaotic behavior and are unidirectionally coupled, forming a master-slave topology. Both the input information signal and the transmitted chaotic signal are digital ones.

Keywords: Nonlinear circuits, Chaotic circuits, Digital chaotic oscillator, Synchronization.

1. Introduction

Nonlinear oscillator synchronization is a process that is frequently encountered in nature, explaining relevant phenomena. A significant property that nonlinear dynamical systems possess is their ability to be synchronized. As a consequence, chaotic system synchronization is encountered in a variety of scientific fields, from astronomy and electronic engineering to social sciences.

Chaotic deterministic signals exhibit several intrinsic features, beneficial to secure communication systems, both analog and digital ones. Two key features of deterministic chaos are the "noise-like" time series and the sensitive dependence on initial conditions [1, 2]. Both of them grant to chaotic signals low probability of detection in chaotic transmissions and low probability of decoding, in case of interception [3].

Due to their possible application for secure internet communications, a number of promising non-linear circuits, demonstrating chaotic behavior, have been presented in the last decade [4-8]. There are two main issues in studying the control of chaotic electronic circuits suitable for secure communications [9]. The first one is the way a non-linear circuit begins to operate in chaotic mode (route to chaos) [2, 10, 11] and the second one is the achievement of synchronization between transmitter-receiver [12, 13].

Since the discovery by Pecora and Carroll that chaotic systems can be synchronized [12], the topic of synchronization of coupled chaotic circuits and systems has been studied intensely [14] and some interesting applications such as broadband communication systems or cryptographic systems have come out of

this research [15-18].

In this paper the system synchronization properties of a chaotic communication system, suitable for secure communication, are examined.

2. Scheme and Circuit description

A very interesting electronic circuit exhibiting chaotic behavior and with potential applications in secure communications, was proposed and numerically examined in [19], while its transmitter has been experimentally studied in [20]. The circuit, of the system under question, is presented in Fig 1.

Both the transmitter and receiver, of this chaotic communication system, are second order non-linear non-autonomous electronic circuits, with their mode of operation depending on the externally applied driving frequency. It has already been found that the transmitter circuit exhibits the period doubling [21, 22] and the intermittency [23, 24] routes to chaos as well as internal crisis [25], in different ranges of driving signal frequency $M(t)$.

The main advantage of this circuit is that it is capable of synchronized chaotic communication, suitable for transmission of digital signal. It should be noted that the transmitted chaotic signal is not analog but a discrete one. Moreover, there is no need of transmitting any special synchronization signal. Synchronization is achieved by the transmitted chaotic information (discrete) signal, itself.

The transmitter and the receiver are identical circuits [19, 20].

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Both the circuits include an integrator-based second-order RC resonance loop, a comparator H (the circuit's non-linear element), an exclusive OR gate, with an input $M(t)$, for the external source and a buffer to avoid overloading of the XOR gate. The external excitation $M(t)$, that is necessary for non-autonomous oscillators, can be either a sequence of square pulses of period $T = 2\pi/\omega$ or a more complex signal, if one wants to encode an arbitrary message, for example. This external excitation serves as the system's information signal.

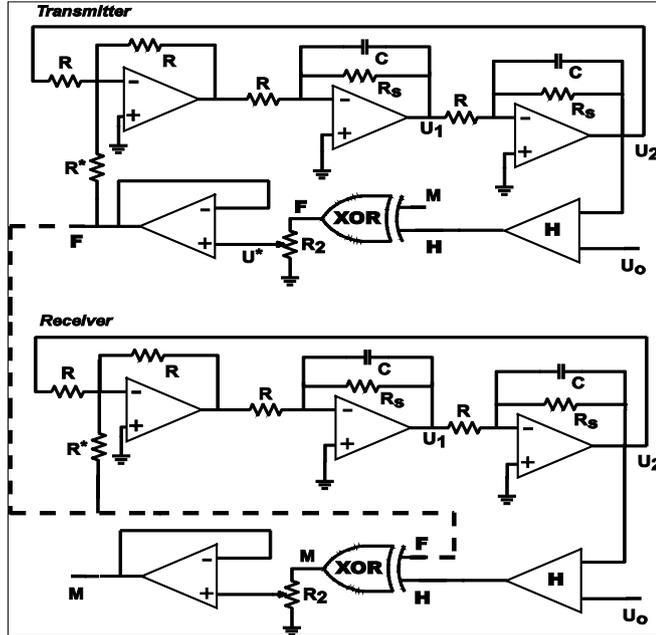


Figure 1. Schematic diagram of the transmitter-receiver system

The main target is the exact reconstruction, at receiver's output, of information signal $M(t)$ applied at the transmitter circuit. This is achieved by synchronously reconstructing U_2 at the transmitter's-receiver's analog output.

The principle of operation is demonstrated below. Here the chaotic pulses $U^*(t) \propto F(y_1, t)$ drive the resonance loops (analog part) of both the transmitter and the receiver. The transmitter system is governed by the following set of equations:

$$\dot{x}_1 = aF(y_1, t) - bx_1 + y_1 \quad (1a)$$

$$\dot{y}_1 = -x_1 - by_1 \quad (1b)$$

$$F(y_1, t) = H(y_1) \oplus M(t) \quad (1c)$$

while the receiver is governed by:

$$\dot{x}_2 = aF(y_2, t) - bx_2 + y_2 \quad (2a)$$

$$\dot{y}_2 = -x_2 - by_2 \quad (2b)$$

It should be noted the same driving term $aF(y_1, t)$, in equations (1a) for the transmitter and (2a) for the receiver, which represents the system's coupling factor. The following substitutions

have been used in the previous systems of equations, since the parameters are written in a dimensionless form:

$$x = \frac{U_1}{U_o}, \quad y = \frac{U_2}{U_o}, \quad t = \frac{1}{RC} \quad (3a)$$

$$\alpha = \frac{U^* \cdot R}{U_o \cdot R^*}, \quad b = \frac{R}{R_s} \quad (3b)$$

$$\omega = \omega_M RC \quad (3c)$$

The symbol \oplus stands for the XOR operation, while H^s stands for the shifted Heaviside function $H^s(y) = H(-y+1)$. $M(t)$ is the normalized square pulse input signal of period $T=2\pi/\omega_1$.

The circuit demonstrates only damped oscillations, as long as no excitation is applied to the XOR gate. The amplitude of the oscillating variables U_1 and U_2 converges exponentially ($\propto e^{-bt}$) to a stable steady state, for all reasonable initial conditions ($U_1^2 + U_2^2 < U_o^2$ or $x^2 + y^2 < 1$) while for a non zero external drive $M(t)$ the circuit becomes periodically forced, exhibiting chaos.

Introducing in the set of equations (1), the error variables $\Delta x = x_2 - x_1$ and $\Delta y = y_2 - y_1$, we obtain the equations governing the error dynamics:

$$\begin{aligned} \Delta \dot{x} &= b\Delta x + \Delta y \\ \Delta \dot{y} &= -\Delta x - b\Delta y \end{aligned} \quad (4)$$

The solution of (4) shows the exponential decrease of the errors for all possible initial errors Δx_0 and Δy_0 . Thus, the synchronization is globally asymptotically stable. This requirement leads to the conclusion that for $\Delta x \rightarrow 0$ and $\Delta y \rightarrow 0$, the corresponding state variables, are robustly synchronized ($x_1 \rightarrow x_2$ and $y_1 \rightarrow y_2$). Consequently, the non-linear functions behave in a synchronous way $H(y_2) \rightarrow H(y_1)$ as well.

This result suggests an extremely simple technique of recovering the signal $M(t)$ at the receiver end. The received signal is applied to the XOR unit of the receiver. Due to the sum mod2 property, the signal $F(y_1, t)$ can be recovered from the chaotic one without any errors, according to:

$$F(y_1, t) \oplus H(y_2) = H(y_1) \oplus M(t) \oplus H(y_2) \rightarrow H(y_1) \oplus M(t) \oplus H(y_1) = M(t) \quad (5)$$

3. Experimental Results

Synchronization between transmitter and receiver was experimentally verified. Both sub-circuits remained synchronized under different conditions, regarding the circuit parameters, as well as, the driving frequency f_i , which was provided by a digital signal generator (HM8130). It should be noted that the driving frequency represents the external digital information that is fed to the communication system.

In this section a typical modulation-demodulation procedure through chaotic synchronization is presented. All signals were monitored by a digital storage oscilloscope (HP54603B), further

connected to a PC for recording and analysis purposes, so that the proper characterization of the circuit behavior could be achieved. Appropriate software, built in NI's LabView environment, was used in order to control all digital instruments used and process the signals acquired [26].

The system's parameters were set to be equal in both the transmitter and the receiver circuits. In order to operate in a chaotic mode, the parameter values, for $U_0=350\text{mV}$ and $U^*=4\text{V}_{p-p}$, were set at $\alpha = 6.35$ and $b = 0.02$. For this set of parameter values, the system exhibits chaotic behavior in various ranges of external excitation f_M (chaotic windows) and undergoes various routes to chaos [21-25].

In order to study the system's synchronization while it operates in a chaotic mode, the driving frequency was set to $f_M=6,222\text{ KHz}$. In Fig. 2 the transmitter's phase portrait (U_1 vs. U_2) is presented. The chaotic nature of signals U_1 and U_2 is evident. Next to the phase portrait, the transmitter's chaotic characterization has been already confirmed in [20].

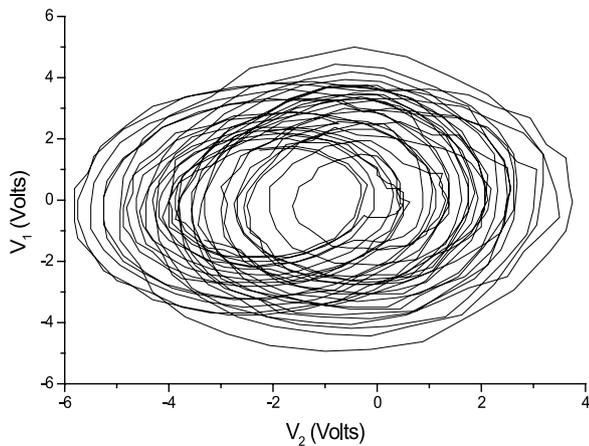
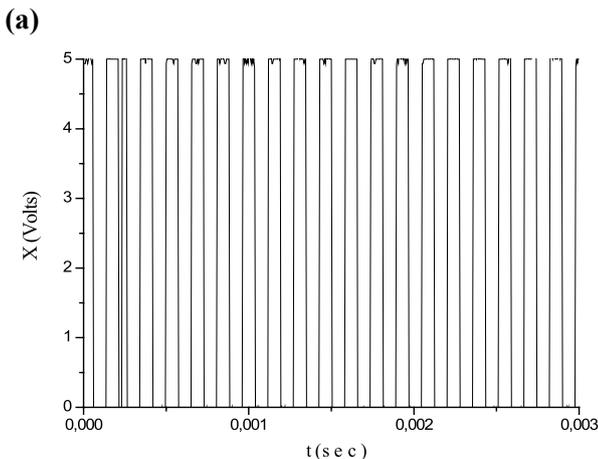


Figure 2. The phase portrait U_1-U_2 characterizing the transmitter's chaotic operation.

In Fig. 3 the driving pulse signal $M(t)$ is shown, together with its power spectrum. The periodic nature of $M(t)$ is obvious. In Fig. 4(a) the signal $F(v_1, t)$ at the transmitter's digital output appears, while in Fig 4(b) the corresponding power spectrum is shown. The power spectrum confirms the wideband nature of the output signal. This wideband signal shows the impossibility of detecting the original information by using simple filtering processes.



According to [27, 28], one can conclude that the present chaotic communication scheme can be secure. Finally, in Fig. 5(a) the recovered signal is presented. Both the signals itself, as well as, the corresponding power spectrum - Fig. 5(b) - demonstrate the fact that the recovery procedure is quite exact.

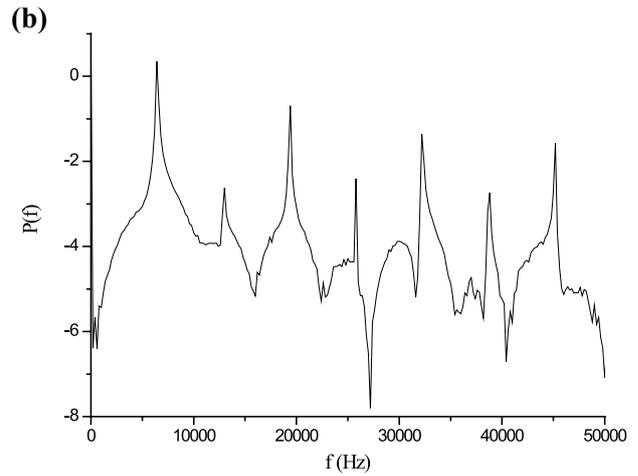


Figure 3. a) Digital input signal $M(t)$ and (b) Its power spectrum (FFT)

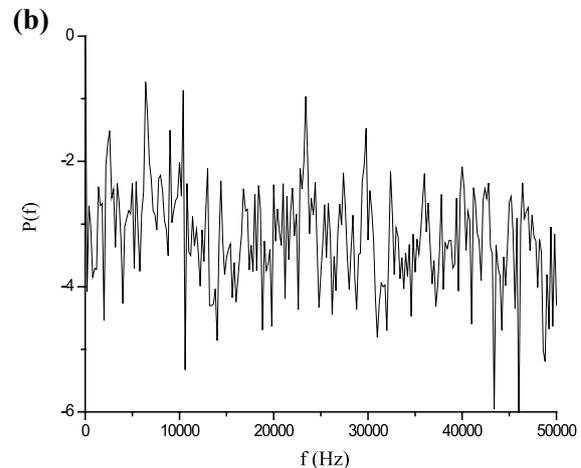
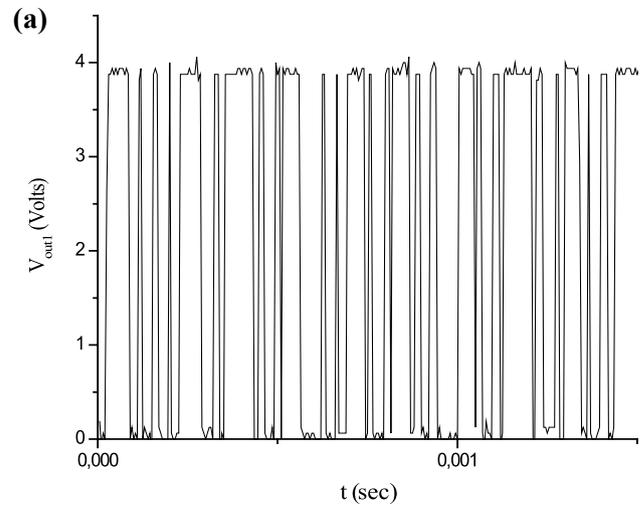


Figure 4. a) The transmitted chaotic signal $F(t)$ and (b) its power spectrum (FFT)

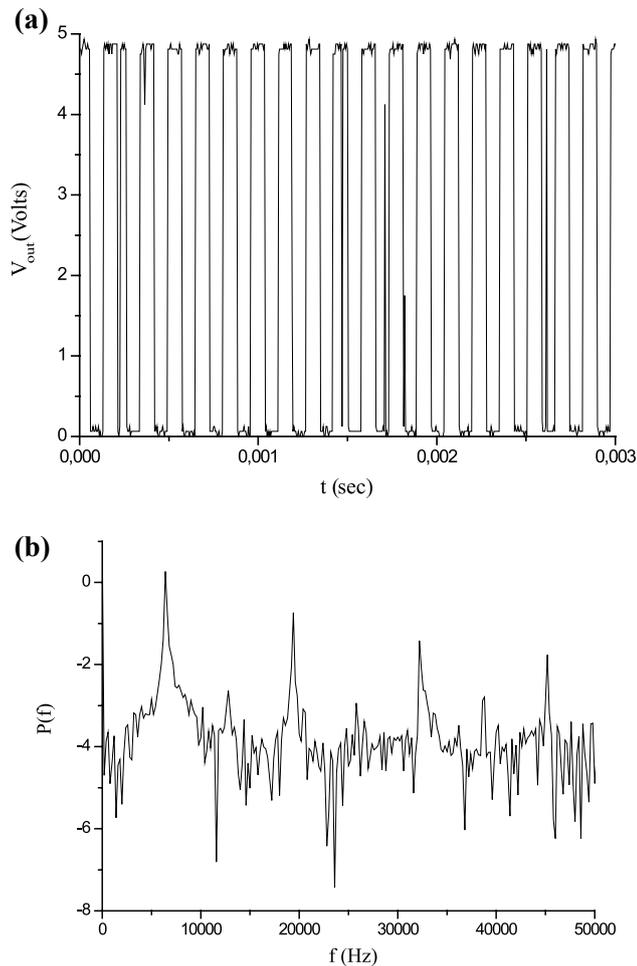


Figure 5. **a)** The recovered signal at the receiver's output and **(b)** its power spectrum (FFT)

It should be mentioned, that the system security depends mainly on three major factors:

(a) The frequency of input signal $M(t)$, since it should be in the range that triggers the circuit to operate in a chaotic mode.

(b) The unfamiliarity of the topology used as a receiver circuit.

(c) The exact knowledge of all the parameters by any would-be intruder.

Conclusions

A scheme capable of secure chaotic digital communication is presented and experimentally studied. Both the information input signal and the transmitted chaotic signal, are discrete (digital) signals. The chaotic nature of the transmitted signal was verified by its power spectrum, while the transmitter's chaotic mode of operation was checked by its phase portrait. The recovered signal, as reconstructed after its synchronized demodulation in the receiver circuit, appears to be the same with the input pulse-series. This is confirmed by its power spectrum, which appears almost the same with the one of the input signal.

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