

## A Secure and Efficient Certificateless Short Signature Scheme

Lin Cheng\* and Qiaoyan Wen

Laboratory of Networking and Switch Technology, Beijing University of Posts and Telecommunications, Beijing 100876, China

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### Abstract

Certificateless public key cryptography combines advantage of traditional public key cryptography and identity-based public key cryptography as it avoids usage of certificates and resolves the key escrow problem. In 2007, Huang et al. classified adversaries against certificateless signatures according to their attack power into normal, strong and super adversaries (ordered by their attack power). In this paper, we propose a new certificateless short signature scheme and prove that it is secure against both of the super type I and the super type II adversaries. Our new scheme not only achieves the strongest security level but also has the shortest signature length (one group element). Compared with the other short certificateless signature schemes which have a similar security level, our new scheme has less operation cost.

**Keywords:** Cryptography, Short signature, Certificateless signature, Bilinear parings

### 1. Introduction

In traditional public key cryptography, a certification authority (CA) issues a certificate to achieve authentication of the user's public key. Identity-based cryptography proposed by Shamir [1] intended to conquer the problem of certificate management in traditional public key cryptography. In identity-based cryptography, the user's public key is derived directly from its name, email-address or other identity information, but it requires a trusted third party called Key Generation Center (KGC) generate the user's private key. Hence, we are confronted with the key escrow problem. At 2003, Al-Riyami and Paterson [2] introduced certificateless public key cryptography, which resolves the inherent key escrow problem in identity-based cryptography, without requiring certificates as used in traditional public key cryptography. In certificateless public key cryptography, the user's public key is independently generated by the user, and the user's private key is a combination partial private key computed by KGC and some user-chosen secret value, in such a way that the key escrow problem can be eliminated without requiring certificates. In certificateless signature, there exist two different Types of attackers. Huang et al. [3] classified the adversaries against certificateless signatures according to their attack power into normal adversary, strong adversary and super adversary (ordered their attack power). As illustrated in [4, 5], the strong Type I adversary might stand in some particular situations. So, a secure certificateless signature scheme should resist the attack of strong Type I/II adversary at least. In [3], the first certificateless short signature scheme (the signature length of one group element) was proposed, which is secure against the normal Type I and super II adversaries.

Shim [4] showed that the certificateless short signatures scheme in [3] is insecure against the strong Type I adversary. Subsequently, Du and Wen [5] presented another short CLS scheme, which was provably secure against the strong Type I adversary and normal Type II adversaries. Choi et al. [6] showed that Du and Wen's certificateless short signature scheme [5] is insecure against the strong Type I adversary and proposed a short CLS scheme which is provably secure against the super Type I and Type II adversaries. Another provably secure short CLS scheme was proposed by Tso et al. [7], however, their defined adversary model is not as powerful as that in Huang et al. [3] and their scheme can not resist the attacks from a strong Type I adversary who can obtain the valid signatures for the replaced public key if he can supply the secret value corresponding to the replaced public key. To the best of our knowledge, Choi et al.'s scheme [6] is the first certificateless short signature scheme which satisfies both the strongest security level and the shortest signature length (one group element). However, their short CLS scheme [6] was proved to be insecure even against the strong Type I adversaries in [8]. In this paper, we propose a new short CLS scheme and prove it is secure against both of the super type I and the super type II adversaries. Compared with the Choi et al.'s scheme [6], our new scheme has less operation cost.

### 2. Preliminaries

In this section, we introduce the related complexity assumption and security model.

#### 2.1 Computational Diffie-Hellman (CDH)

Given a generator  $P$  of an additive cyclic group  $G_1$ , and  $(aP, bP)$  for some unknown  $a, b \in \mathbb{Z}_q^*$ . The CDH problem is

\* E-mail address: stonewoods302@163.com

to compute  $abP$ . Let  $C$  be a probabilistic polynomial time algorithm. We define  $C$ 's advantage in solving the CDH problem by  $Adv(C) = Pr[B(P, aP, bP) = abP]$ .

The CDH assumption states that for every probabilistic polynomial time algorithm  $C$ ,  $Adv(C)$  is negligible.

## 2.2 Security model

In the security model defined in [3, 6], each super adversary  $A \in \{A_I, A_{II}\}$  may issue the following queries.

**Extract-Partial-Private-Key ( $ID$ )**. When  $A$  supplies an identity  $ID$ , challenger  $C$  computes the corresponding partial private key  $D_{ID}$  for this identity and returns  $D_{ID}$  to  $A$ .

**Extract-Public-Key ( $ID$ )**. When  $A$  supplies an identity  $ID$ , challenger  $C$  returns the corresponding public key  $PK_{ID}$  to  $A$ .

**Extract-Secret-Value ( $ID$ )**. When  $A$  supplies an identity  $ID$ , challenger returns  $x_{ID}$  to  $A$ . Note that, the secret value  $x_{ID}$  is used to generate the original public key of  $ID$ . If the public key associated with  $ID$  has been replaced earlier,  $A$  cannot receive any response.

**Replace-Public-Key ( $ID, PK'_{ID}$ )**. When  $A$  supplies an identity  $ID$  and a new valid public key value  $PK'_{ID}$ , challenger  $C$  replaces the current public key with  $PK'_{ID}$ .

**Super-Sign ( $ID, m$ )**. When  $A$  supplies an identity  $ID$  and a message  $m$ , challenger  $C$  responds with a signature  $\delta$  such that  $1 \leftarrow Verify(params, ID, PK'_{ID}, m, \delta)$ , where  $PK'_{ID}$  is the current public key corresponding to  $ID$  and it may be replaced by the Replace-Public-Key query.

**Game I**. This game is performed between a challenger  $C$  and a Type I adversary  $A_I$  for a CLS scheme as follows.

**Initialization**. Challenger  $C$  runs algorithm **Setup** to generate a master secret key  $msk$ , and public system parameters  $params$ .  $C$  then gives  $params$  to  $A_I$  and keeps  $msk$  secret. Note that  $A_I$  does not know the master key  $msk$ .

**Queries**. In this phase,  $A_I$  adaptively performs a polynomially bounded number of oracle queries: Extract-Partial-Private-Key, Extract-Secret-Value, Request-Public-Key, Replace-Public-Key and Super-Sign.

**Output**. Eventually,  $A_I$  outputs  $(ID^*, m^*, \delta^*)$ , where  $ID^*$  is the identity of a target user,  $m^*$  is a message, and  $\delta^*$  is a signature for  $m^*$ .  $A_I$  wins the game if

- (1) Extract-Partial-Private-Key ( $ID^*$ ) query has never been queried.
- (2) Super-Sign ( $ID^*, m^*$ ) query has never been queried.
- (3)  $1 \leftarrow Verify(params, ID^*, PK_{ID^*}, m^*, \delta^*)$ , where  $PK_{ID^*}$  which may be replaced by  $A_I$  is the current public key of  $ID^*$ .

**Game II**. This game is performed between a challenger  $C$  and a Type I adversary  $A_I$  for a CLS scheme as follows.

**Initialization**. Challenger  $C$  runs algorithm **Setup** to generate a master secret key  $msk$ , and public system

parameters  $params$ .  $C$  then gives  $params$  and  $msk$  to  $A_{II}$ .

**Queries**. In this phase,  $A_{II}$  can adaptively issue Extract-Secret-Value, Request-Public-Key and Replace-Public-Key queries to  $C$ . In addition, he can also issue only one type of the following queries: Normal-Sign, Strong-Sign, and Super-Sign.

**Output**. Eventually,  $A_{II}$  outputs  $(ID^*, m^*, \delta^*)$ , where  $ID^*$  is the identity of a target user,  $m^*$  is a message, and  $\delta^*$  is a signature for  $m^*$ .  $A_{II}$  wins the game if

- (1) Extract-Partial-Private-Key ( $ID^*$ ) query has never been queried.
- (2) Super-Sign ( $ID^*, m^*$ ) query has never been queried.
- (3)  $1 \leftarrow Verify(params, ID^*, PK_{ID^*}, m^*, \delta^*)$ , where  $PK_{ID^*}$  is the original public key of  $ID^*$ .

**Definition 1**. We say that a CLS scheme is existentially unforgeable, if no polynomially bounded adversaries  $A$  ( $A_I$  and  $A_{II}$ ) have non-negligible advantage of winning the above game.

## 3. New Short Certificateless Signature Scheme

In this section, we propose a new short CLS scheme which is secure against the super Type I/II adversary.

### 3.1 Construction

**Setup**. Let  $(G_1, +)$  and  $(G_2, \cdot)$  be two cyclic groups of prime order  $q$  and  $P$  is a generator of  $G_1$ . Given a bilinear pairing  $e: G_1 \times G_1 \rightarrow G_2$  and three distinct hash functions  $H_1, H_2$  and  $H_3: \{0,1\}^* \rightarrow G_1$ ,  $H_1: \{0,1\}^* \rightarrow Z_q^*$ ,  $H_2: \{0,1\}^* \rightarrow G_1$ ,  $H_3: \{0,1\}^* \rightarrow G_1$ . The KGC selects  $s \in Z_q^*$  uniformly as master-key and sets  $P_{pub} = sP$ . The public parameters list

$params = \{G_1, G_2, e, q, P, P_{pub}, H_1, H_2, H_3\}$ . The master secret key  $msk = s$ .

**Partial-Private-Key-Extract**. On input  $params$ , master key  $s$ ,  $ID \in \{0,1\}^*$ , KGC carries out the following for generating a partial private  $d_{ID}$  for a user with identity  $ID$ .

Choose at random  $r \in Z_q^*$ , compute  $R_{ID} = rP$ ,  $h_1 = H_1(R_{ID}, ID)$  and  $d_{ID} = r + h_1s \bmod q$ . Return  $(R_{ID}, d_{ID})$  to the user. The user can check its correctness by checking whether  $d_{ID}P = R_{ID} + h_1P_{pub}$ .

**Set-Secret-Value**. The user selects a random value  $x_{ID} \in Z_q^*$  as his secret key.

**Set-Public-Key**. The user computes  $Y_{ID} = x_{ID}P$ , then sets his public key  $PK_{ID} = (R_{ID}, Y_{ID})$ .

**CL-Sign**. On inputs  $params$ , a message  $m \in \{0,1\}^*$ , signer's identity  $ID$  and his partial private  $d_{ID}$  and secret key  $x_{ID}$ , the signer computes  $\delta = d_{ID}H_2(m, ID, R_{ID}, Y_{ID}) + x_{ID}H_3(m, ID, R_{ID}, Y_{ID})$ .

**CL-Verify.** Given  $params$ ,  $PK_{ID}$ , message  $m$ , signer's identity  $ID$  and signature  $\delta$ , the verifier computes

$$h_1 = H_1(R_{ID}, ID), h_2 = H_2(m, ID, R_{ID}, Y_{ID}), h_3 = H_3(m, ID, R_{ID}, Y_{ID}).$$

Accept the signature if the following equation holds:  
 $e(\delta, P) = e(R_{ID} + h_1 P_{pub}, h_2) e(Y_{ID}, h_3).$

### 3.2 Proof of security

**Theorem 1.** The proposed certificateless signature scheme is existential unforgeable against a super adversary  $A_I$  under the CDH assumption.

**Proof.** Suppose there exists a super Type I adversary  $A_I$  which has advantage  $\varepsilon$  in attacking our short CLS scheme. We want to build an algorithm  $C$  that uses  $A_I$  to solve the CDH problem. Suppose that  $C$  is given  $(P, aP, bP)$  as an instance of the CDH problem. Its goal is to compute  $abP$ .  $C$  will run  $A_I$  as a subroutine and act as  $A_I$ 's challenger. We describe the simulation as follows.

**Initialization.**  $C$  sets  $P_{pub} = aP$  and provides  $A_I$  with  $\{G_1, G_2, e, q, P, P_{pub}, H_1, H_2, H_3\}$  as public parameters, where  $H_1, H_2, H_3$  are random oracles controlled by  $C$ .

**Queries.** In the query phase,  $C$  responds  $A_I$ 's queries as follows:

**$H_1$  query:**  $C$  maintains a  $H_1$  list of tuples  $(ID_i, R_{ID_i}, t_{li})$ . When  $A_I$  makes  $H_1$  query on  $(ID_i, R_{ID_i})$ ,  $C$  looks up the  $H_1$  list and does the following:

1. If  $H_1$  list contains  $(ID_i, R_{ID_i}, t_{li})$ ,  $C$  returns  $t_{li}$  to  $A_I$ .
2. Otherwise,  $C$  picks  $t_{li} \in Z_p^*$  at random, adds  $(ID_i, R_{ID_i}, t_{li})$  to  $H_1$  list and returns  $t_{li}$  to  $A_I$ .

**$H_2$  query:**  $C$  maintains a  $H_2$  list of tuples  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ . When  $A_I$  makes  $H_2$  query on  $(m_i, ID_i, R_{ID_i}, Y_{ID_i})$ ,  $C$  looks up the  $H_2$  list and does the following:

1. If  $H_2$  list contains  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ ,  $C$  returns  $T_{2i}$  to  $A_I$ .
2. Otherwise,  $C$  picks  $t_{2i} \in Z_p^*$  at random, computes  $T_{2i} = t_{2i}bP$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$  to  $H_2$  list and returns  $T_{2i}$  to  $A_I$ .

**$H_3$  query:**  $C$  maintains a  $H_3$  list of tuples  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$ . When  $A_I$  makes  $H_3$  query on  $(m_i, ID_i, R_{ID_i}, Y_{ID_i})$ ,  $C$  looks up the  $H_3$  list and does the following:

1. If  $H_3$  list contains  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$ ,  $C$  returns  $T_{3i}$  to  $A_I$ .
2. Otherwise,  $C$  picks  $t_{3i} \in Z_p^*$  at random, computes  $T_{3i} = t_{3i}P$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_3$  list and returns  $T_{3i}$  to  $A_I$ .

**Extract-Partial-Private-Key ( $ID_i$ ) query:**  $C$  maintains a partial key list of tuples  $(ID_i, R_{ID_i}, d_{ID_i})$ . Suppose  $A_I$  makes at most  $q_{pp}$  queries to the partial private key extraction oracle. First,  $C$  chooses  $j \in [1, q_{pp}]$  randomly. When  $A_I$  makes a partial key extraction query on  $ID_i$ .

1. If  $i = j$  (we let  $ID_i = ID^*$  at this point), then  $C$  outputs "failure" and halts because it is unable to coherently answer the query.

2. Otherwise ( $i \neq j$ ),  $C$  looks up the partial key list. If partial key list contains  $(ID_i, R_{ID_i}, d_{ID_i})$ ,  $C$  returns  $(R_{ID_i}, d_{ID_i})$  to  $A_I$ . Otherwise,  $C$  chooses  $t_{li}, d_{li} \in Z_q^*$  at random, and sets  $R_{ID_i} = d_{li}P - t_{li}P_{pub}$ ,  $d_{ID_i} = d_{li}$ ,  $H_1(R_{ID_i}, ID_i) = t_{li}$ .  $C$  adds  $(ID_i, R_{ID_i}, t_{li})$  to  $H_1$  list and  $(ID_i, R_{ID_i}, d_{ID_i})$  to partial key list, and returns  $(R_{ID_i}, d_{ID_i})$  to  $A_I$ . Note that  $(R_{ID_i}, d_{ID_i})$  is a validly partial private key for the identity  $ID_i$  since it satisfies the equation  $d_{ID_i}P = R_{ID_i} + h_1(R_{ID_i}, ID_i)P_{pub}$ .

**Request-Public-Key ( $ID_i$ ) query:**  $C$  maintains a public key list of tuples  $(ID_i, (R_{ID_i}, Y_{ID_i}))$ . When  $A_I$  makes a public key request query on  $ID_i$ ,  $C$  looks up public key list and does the following:

1. If public key list contains  $(ID_i, (R_{ID_i}, Y_{ID_i}))$ ,  $C$  returns  $PK_{ID_i} = (R_{ID_i}, Y_{ID_i})$  to  $A_I$ .
2. Otherwise,  $C$  does the following:
  - (a) If partial key list contains  $(ID_i, R_{ID_i}, d_{ID_i})$ ,  $C$  picks  $x_{ID_i} \in Z_p^*$  at random and computes  $Y_{ID_i} = x_{ID_i}P$ ; adds  $(ID_i, x_{ID_i})$  to secret value list and  $(ID_i, R_{ID_i}, Y_{ID_i})$  to public key list; returns  $PK_{ID_i} = (R_{ID_i}, Y_{ID_i})$  to  $A_I$ .
  - (b) Otherwise,  $C$  gets a partial key  $(R_{ID_i}, d_{ID_i})$  by making partial key extraction query on  $ID_i$ ; then  $C$  picks  $x_{ID_i} \in Z_p^*$  at random and computes  $Y_{ID_i} = x_{ID_i}P$  and adds  $(ID_i, R_{ID_i}, d_{ID_i})$  to partial key list and  $(ID_i, x_{ID_i})$  to secret value list and  $(ID_i, R_{ID_i}, Y_{ID_i})$  to public key list; finally  $C$  returns  $PK_{ID_i} = (R_{ID_i}, Y_{ID_i})$  to  $A_I$ .

**Replace-Public-Key ( $ID_i, PK'_{ID_i}$ ) query:** When  $A_I$  makes this query on  $ID_i$ , if public key list contains  $PK'_{ID_i}$ ,  $C$  sets  $PK_{ID_i} = PK'_{ID_i}$ . Otherwise,  $C$  makes a secret value query on  $ID_i$ ,  $C$  then sets  $PK_{ID_i} = PK'_{ID_i}$ .

**Extract-Secret-Value ( $ID_i$ ) query:**  $C$  maintains a secret value list of tuples  $(ID_i, x_{ID_i})$ . When  $A_I$  makes this query on  $ID_i$ ,  $C$  looks up secret value list and does the following.

1. If the secret value list contains  $ID_i, x_{ID_i}$ , C returns  $x_{ID_i}$ .

2. Otherwise, C picks  $r_{ID_i}, x_{ID_i} \in Z_p^*$  at random and computes  $R_{ID_i} = r_{ID_i}P, Y_{ID_i} = x_{ID_i}P$ ; adds  $(ID_i, x_{ID_i})$  to secret value list and  $(ID_i, R_{ID_i}, Y_{ID_i})$  to public key list. C then returns  $x_{ID_i}$ .

**Super-Sign** ( $m_i, ID_i$ ) **query**: When  $A_I$  makes this query on  $(ID_i, m_i)$ , C performs as follows:

1. If  $ID_i = ID^*$ , C picks two random values  $t_{1i}, t_{3i} \in Z_p^*$ , sets  $h_2 = -R_{ID_i} - t_{1i}aP$  and  $\delta = t_{3i}Y_{ID_i}$  (C halts and outputs “failure” if  $H_2$  turns out to have already been defined for  $(m_i, ID_i, R_{ID_i}, Y_{ID_i})$ ). C then returns  $\delta$  and adds  $(ID_i, R_{ID_i}, t_{1i})$ ,  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_1$  list,  $H_3$  list, respectively.

2. Otherwise, C picks two random values  $t_{2i}, t_{3i} \in Z_p^*$  and computes  $\delta = d_{ID_i}t_{2i}bP + t_{3i}Y_{ID_i}$ . C then returns  $\delta$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ ,  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_2$  list,  $H_3$  list, respectively.

**Output**: Eventually,  $A_I$  outputs a forgery signature  $\delta^*$  on message  $m^*$  with respect to  $(ID^*, PK_{ID^*})$ . If  $ID^* \neq ID_j$ , then C outputs “failure” and stops. Otherwise, C finds out an item  $(ID^*, R_{ID^*}, t_{1i}^*)$  in the  $H_1$  list, an item  $(m^*, ID^*, R_{ID^*}, Y_{ID^*}, t_{2i}^*, T_{2i})$  in the  $H_2$  list, and an item  $(m^*, ID^*, R_{ID^*}, Y_{ID^*}, t_{3i}^*, T_{3i})$  in the  $H_3$  list. Note that the list  $H_1, H_2, H_3$  must contain such entries with overwhelming probability (otherwise C outputs “failure” and stops). Note that  $H_1(R_{ID^*}, ID^*) = t_{1i}^*P$ ,  $H_2(m^*, ID^*, R_{ID^*}, Y_{ID^*}) = t_{2i}^*bP$ ,  $H_3(m^*, ID^*, R_{ID^*}, Y_{ID^*}) = t_{3i}^*P$ . If  $A_I$  succeeds in the game, then

$$\begin{aligned} e(\delta^*, P) &= e(R_{ID_i^*} + h_1^*P_{pub}, h_2^*)e(Y_{ID_i^*}, h_3^*) \\ &= e(R_{ID_i^*}, h_2^*)e(h_1^*P_{pub}, h_2^*)e(Y_{ID_i^*}, h_3^*) \\ &= e(R_{ID_i^*}, t_{2i}^*bP)e(t_{1i}^*aP, t_{2i}^*bP)e(Y_{ID_i^*}, t_{3i}^*P) \end{aligned} \quad (1)$$

Using Forking Lemma [9], after replaying  $A_I$  with the same random tape, C obtains another valid signed message  $(m^*, \delta'^*)$ . The message will satisfy

$$\begin{aligned} e(\delta'^*, P) &= e(R_{ID_i^*} + h_1'^*P_{pub}, h_2'^*)e(Y_{ID_i^*}, h_3'^*) \\ &= e(R_{ID_i^*}, h_2'^*)e(h_1'^*P_{pub}, h_2'^*)e(Y_{ID_i^*}, h_3'^*) \\ &= e(R_{ID_i^*}, t_{2i}'bP)e(t_{1i}'aP, t_{2i}'bP)e(Y_{ID_i^*}, t_{3i}'P) \end{aligned} \quad (2)$$

From the Eqs. (1) and (2), C can obtain the solution of the CDH problem by computing

$$abP = \frac{t_{2i}'\delta^* - t_{2i}\delta'^* - (t_{2i}'t_{3i}^* - t_{2i}t_{3i}')Y_{ID_i^*}}{t_{2i}'t_{1i}'t_{2i}^* - t_{2i}t_{1i}^*t_{2i}'}$$

**Theorem 2.** The proposed certificateless signature scheme is existential unforgeable against a super adversary  $A_{II}$  under the CDH assumption.

**Proof.** Suppose there exists a super Type II adversary  $A_{II}$  which has advantage  $\varepsilon$  in attacking our short CLS scheme. We want to build an algorithm C that uses  $A_{II}$  to solve the CDH problem. Suppose that C is given  $(P, aP, bP)$  as an instance of the CDH problem. Its goal is to compute  $abP$ . C will run  $A_{II}$  as a subroutine and act as  $A_{II}$ 's challenger. We describe the simulation as follows.

**Initialization.** C picks a random  $s \in Z_q^*$  and sets  $P_{pub} = sP$ , where  $s$  is the master key. C gives system parameters with master key to  $A_{II}$ .

**Queries.** In the query phase, C responds  $A_{II}$ 's queries as follows:

**$H_1$  Queries:** C maintains a  $H_1$  list of tuples  $(ID_i, R_{ID_i}, t_{1i})$ . When  $A_{II}$  makes  $H_1$  query on  $(ID_i, R_{ID_i})$ , C looks up the  $H_1$  list and does the following:

1. If  $H_1$  list contains  $(ID_i, R_{ID_i}, t_{1i})$ , C returns  $t_{1i}$  to  $A_{II}$ .
2. Otherwise, C picks  $t_{1i} \in Z_p^*$  at random, and adds  $(ID_i, R_{ID_i}, t_{1i})$  to  $H_1$  list and returns  $t_{1i}$  to  $A_{II}$ .

**$H_2$  Queries:** C maintains a  $H_2$  list of tuples  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ . When  $A_{II}$  makes  $H_2$  query on  $(m_i, ID_i, R_{ID_i}, Y_{ID_i})$ , C looks up the  $H_2$  list and does the following:

1. If  $H_2$  list contains  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ , C returns  $t_{2i}P$  to  $A_{II}$ .
2. Otherwise, C picks  $t_{2i} \in Z_p^*$  at random, and computes  $T_{2i} = t_{2i}P$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$  to  $H_2$  list and returns  $T_{2i}$  to  $A_{II}$ .

**$H_3$  Queries:** C maintains a  $H_3$  list of tuples  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$ . When  $A_{II}$  makes  $H_3$  query on  $(m_i, ID_i, R_{ID_i}, Y_{ID_i})$ , C looks up the  $H_3$  list and does the following:

1. If  $H_3$  list contains  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$ , C returns  $T_{3i}$  to  $A_{II}$ .
2. Otherwise, C picks  $t_{3i} \in Z_p^*$  at random, and computes  $T_{3i} = t_{3i}aP$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_3$  list and returns  $T_{3i}$  to  $A_{II}$ .

**Request-Public-Key** ( $ID_i$ ) **query**: C maintains a public key list of tuples  $(ID_i, (R_{ID_i}, Y_{ID_i}))$ . Suppose  $A_{II}$  makes at most  $q_{pk}$  queries to the public key request oracle. First, C chooses  $j \in [1, q_{pk}]$  randomly. When  $A_{II}$  makes a

public key request query on  $ID_i$ , C looks up the public key list and does the following:

1. If public key list contains  $(ID_i, (R_{ID_i}, Y_{ID_i}))$ , C returns

$$PK_{ID_i} = (R_{ID_i}, Y_{ID_i}) \text{ to } A_{II}.$$

2. If  $i = j$  (we let  $ID_i = ID^*$  at this point), C sets  $Y_{ID_i} = bP$  and picks  $r_{ID_i}$  at random and computes  $R_{ID_i} = r_{ID_i}P$ , finally C returns  $PK_{ID_i} = (R_{ID_i}, Y_{ID_i})$  to  $A_{II}$ .

3. Otherwise ( $i \neq j$ ), C picks  $r_{ID_i}, x_{ID_i} \in Z_p^*$  at random and computes  $R_{ID_i} = r_{ID_i}P, Y_{ID_i} = x_{ID_i}P$ ; adds  $(ID_i, x_{ID_i})$  to secret value list and  $(ID_i, R_{ID_i}, Y_{ID_i})$  to public key list; returns  $PK_{ID_i} = (R_{ID_i}, Y_{ID_i})$  to  $A_{II}$ .

**Replace-Public-Key** ( $ID_i, PK'_{ID_i}$ ) **query**: When  $A_{II}$  makes this query on  $ID_i$ , if public key list contains  $PK'_{ID_i}$ , C sets  $PK_{ID_i} = PK'_{ID_i}$ . Otherwise, C makes a public key query on  $ID_i$ , C then sets  $PK_{ID_i} = PK'_{ID_i}$ .

**Extract-Secret-Value** ( $ID_i$ ) **query**: C maintains a secret value list of tuples  $(ID_i, x_{ID_i})$ . When  $A_{II}$  makes this query on  $ID_i$ , C does the following:

1. Run the public key request taking  $ID_i$  as input to get a tuple  $(ID_i, R_{ID_i}, Y_{ID_i})$ .

2. If  $i \neq j$ , search secret value list  $(ID_i, x_{ID_i})$  to get  $x_{ID_i}$ , and then return  $SK_{ID_i} = (d_{ID_i}, x_{ID_i})$  to  $A_{II}$ .

3. Otherwise, return “failure” and terminate.

**Super-Sign** ( $m_i, ID_i$ ) **query**: When  $A_{II}$  makes this query on  $(ID_i, m_i)$ , C first finds  $(ID_i, R_{ID_i}, Y_{ID_i})$  from public key list, then performs as follows:

1. If  $ID_i \neq ID^*$ , C picks two random values  $t_{2i}, t_{3i} \in Z_p^*$  and computes  $\delta = d_{ID_i}t_{2i}P + t_{3i}bP$ . C then returns  $\delta$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ ,  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_2$  list,  $H_3$  list, respectively.

2. Otherwise, C picks two random values  $t_{2i}, t_{3i} \in Z_p^*$  and computes  $\delta = d_{ID_i}t_{2i}P + t_{3i}Y_{ID_i}$ . C then returns  $\delta$  and adds  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{2i}, T_{2i})$ ,  $(m_i, ID_i, R_{ID_i}, Y_{ID_i}, t_{3i}, T_{3i})$  to  $H_2$  list,  $H_3$  list, respectively.

**Output**. Eventually,  $A_{II}$  outputs a forgery signature  $\delta^*$  on message  $m^*$  with respect to  $(ID^*, PK_{ID^*})$ . If  $ID^* \neq ID_j$ ,

C outputs “failure” and stops. The following equation holds because the signature is valid.

$$\begin{aligned} e(\delta^*, P) &= e(R_{ID_i^*} + h_1^*P_{pub}, h_2^*)e(Y_{ID_i^*}, h_3^*) \\ &= e(R_{ID_i^*} + t_{1i}^*P_{pub}, t_{2i}^*P)e(bP, t_{3i}^*aP) \end{aligned}$$

C can obtain the solution of the CDH problem as  $abP = (t_{3i}^*)^{-1}(\delta^* - t_{2i}^*(R_{ID_i^*} + t_{1i}^*P_{pub}))$ .

### 3.3. Performance Analysis

The existing certificateless short signature scheme (the signature length of one group element) can be provably secure against both of the super type I and the super type II adversaries is proposed by Choi et al [6]. Table 1 summarizes the comparisons of our scheme with Choi et al.’s scheme [6] in the signature and verification stages.  $H$  denotes the Hash function operation,  $e$  denotes a pairing operation, and  $P$  denotes the scalar multiplication operation.

**Table 1** Efficiency comparison

Schemes	Hash	Pairing	scalar multiplication
[6]	8 $H$	3 $e$	5 $P$
Ours	5 $H$	3 $e$	3 $P$

From Table 1, we know our scheme is more efficient than Choi et al.’s scheme [6].

### 4. Conclusion

In this paper, we propose a new short CLS scheme and prove its security in the random oracle model under the computational Diffie-Hellman assumption. Our new scheme satisfies both the strongest security level and the shortest signature length (one group element). Compared with the short CLS scheme proposed by Choi et al. [6] which has a similar security level, our new scheme has less operation cost. Thus, our scheme can be applied in low bandwidth communication, low storage and low computation environments.

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