

Estimation of Rotor and Stator Resistance for Induction Motor Drives using Second order of Sliding Mode Controller

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Abstract

The continues operation of vector controlled induction motor drives faces the problem of the stator and rotor resistance variation due to saturation, skin effect or in temperature variations. These resistance variations affect the controller performance. This paper illustrates about a new closed loop approach for estimation followed by compensation of the stator and rotor resistance of induction motor by using the second order sliding mode controller. The motor resistances estimated by online and the error between the actual and desired state variables of the induction motor track the sliding surface, the proposed method are based on the rigorous Lyapunov stability criteria. The simulation results show that the high frequency variation in the output waveform reduces as compared to the classical sliding mode controller and the mathematical analysis is simple to reduce the complexity faces in the higher order controller. For the estimation of the control variables of proposed algorithm only current measurement is needed and the controller is independent of the unknown parameter variation as the property of the sliding mode controller. The proposed method has been analyzed and verified with the help of Matlab/Simulink.

Keywords: Induction Motor (IM); Sliding mode controller (SMC); Parameter; Compensation; Estimation.

1. Introduction

Induction motor drive is now acquiring an enormous attention in the field of electric drive as well as in dynamic control due to its high dynamic response and its low cost. The vector controlled method is generally used due to its simplicity and fast response. The dynamic model of induction motor is precisely nonlinear, so having control over induction motor is a challenging problem which attracted much attention. Moreover, with the operation of the drives the parameters (resistance and inductance) vary due to saturation, skin effect or to variations in the temperature. In vector controlled induction motor drives the variation in inductance is negligible because it operates at constant flux, so the only resistance of the rotor and stator windings are variable. The performance of the drives influence by the variation of the resistances to omit this problem and improve the performance of the drive the controller scheme independent of the variation in parameters or developed some algorithm that can estimate and compensate the parameters simultaneously.

The rotor and stator resistance of induction motor vary with the temperature variation due to motor heating, many researchers develop an algorithm to predict the stator resistance [1] -[3] by using the microcontroller and online estimation but these are unstable in low speed range or the regenerative mode of the electric drives. Estimation of rotor

resistance of the induction motor is important because strongly influences the speed of the induction motor. Rotor resistance estimated by using Reactive power error method, by torque error method and by error function based on stator voltage [4] -[7] these techniques take the large convergence time and a large harmonic present in the supply voltage that fluctuate the estimated parameters. Although all the above techniques estimate the stator or a rotor resistance individually where as the controller performance affects by variation of a stator and a rotor resistance both, so for improving the performance of the controller both stator and rotor resistance estimation require. In papers [8] -[10] both stator and rotor resistances are estimated, mainly used the online and observer based methods, these methods are complex it bounded the stator current. Fuzzy logic and artificial neural network are also used to estimate the rotor and stator resistance, but in this method proper design of fuzzy rules and the adjustment of the weight require [11] -[14]. Even many optimization methods like genetic algorithm, partial swam optimization methods are also used to estimate the resistance of the induction motor, but all these optimization methods are offline methods [15] -[18]. In the real world application any optimization technique requires a long time to run and a large memory and it is impossible to find exact result, the result can be only near the global extreme.

Sliding mode controller (SMC) is a robust controller, which is uncertain with the parameter variation. Most of the researchers use SMC observer for estimation the stator and rotor resistances [19]-[22] but they are higher order, due to this the complexity of the system increases. Even the

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classical SMC technique is also applied to estimate the resistance of the IM in the sensorless IM control drives [23]. The classical SMC faces the problem of chattering [24]-[25]. Many researchers work on to eliminate the chattering [26]. In recent years a robust software sensor for the IM drives is developed for estimation the stator resistance that improve the performance of the drives [27] but that software only estimate the stator resistance.

In this paper a second order SMC with the new proposed control law based on lyapunov stability theory [28] is used to estimate and also compensate the rotor and stator resistance, using online adaptation method. A singular perturbation theory is used to reduce the order of the induction motor from fifth order to second order [29]-[31] and the second order SMC in place of 9th or higher order decreases the complexity of the system and make it simple. The chattering problem is mitigates with the use of the second order SMC.

2. Mathematical Modelling of Induction motor

The Mathematical model of induction motor in the dq coordinate is given by [32].

$$\frac{d}{dt} \begin{bmatrix} i_{ds} \\ i_{qs} \\ \psi_{dr} \\ \psi_{qr} \end{bmatrix} = \begin{bmatrix} -a_1 & \omega_e & a_2 & a_3 \omega_r \\ -\omega_e & -a_1 & a_3 \omega_r & a_2 \\ a_5 & 0 & -a_4 & \omega_{sl} \\ 0 & a_5 & -\omega_{sl} & -a_4 \end{bmatrix} \begin{bmatrix} i_{ds} \\ i_{qs} \\ \psi_{dr} \\ \psi_{qr} \end{bmatrix} + \begin{bmatrix} c & 0 \\ 0 & c \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{ds} \\ v_{qs} \end{bmatrix} \quad (1)$$

$$T_e - T_L = J \frac{d\omega_m}{dt} + B\omega_m \quad (2)$$

where (i_{ds}, i_{qs}) , (v_{ds}, v_{qs}) , (ψ_{dr}, ψ_{qr}) are stator current, stator voltage, and rotor flux respectively, these are normalized by the mutual inductance L_m in dq coordinate. Whereas ω_r, T_e, T_L and ω_e is the rotor speed (rad/s), motor torque (Nm), load torque (Nm) and angular frequency of the stator current (rad/s) respectively.

Where,

$$a_1 = \frac{1}{\sigma L_s} \left(R_s + \frac{R_r L_m^2}{L_r^2} \right);$$

$$a_2 = \frac{1}{\sigma L_s} \frac{R_r L_m^2}{L_r^2}$$

$$a_3 = \frac{1}{\sigma L_s} \frac{L_m}{L_r}; a_5 = \frac{R_r L_m}{L_r}; a_4 = \frac{R_r}{L_r};$$

$$c = \frac{1}{\sigma L_s}$$

$$\omega_{sl} = \omega_e - \omega_r; \omega_{sl} = a_5 \frac{i_{qs}}{\psi_{dr}} \quad (3)$$

are constants, R_s is the stator resistance, R_r is the rotor resistance, L_s is the stator inductance, L_r is the rotor inductance, L_m is the mutual inductance, p is the number of poles pairs, and J is the moment of inertia of the rotor.

As we can see from equation (1) and (2), the mathematical equation of induction motor is nonlinear and

it is the fifth order of equations, in which many variables are known. To make a system simpler a singular perturbation theory is used to reduce the order of the induction motor [29-31]. According to that theory the part of the system which operated at slower speed assume as constant. In induction motor drive system the mechanical dynamics operated at much slower speed as compare to the current dynamics and electromagnetic dynamics. So, the flux and rotor speed assumed to be constant and drive the state space equation of the induction motor as given in equation (4). The order of the equation reduces to second order in which the states of the equations are only the d-axis stator and q-axis stator currents.

$$\frac{d}{dt} \begin{bmatrix} i_{ds} \\ i_{qs} \end{bmatrix} = \begin{bmatrix} a_1 & \omega_e & a_2 & a_3 \omega_r \\ -\omega_e & a_1 & -a_3 \omega_r & a_2 \end{bmatrix} \begin{bmatrix} i_{ds} \\ i_{qs} \\ \psi_{dr} \\ \psi_{qr} \end{bmatrix} + \begin{bmatrix} c & 0 \\ 0 & c \end{bmatrix} \begin{bmatrix} v_{ds} \\ v_{qs} \end{bmatrix} \quad (4)$$

In field orientated control of induction motor, to achieve field orientation, the q-axis torque component perpendicular to the rotor flux, and the d-axis flux component aligned in the direction of it. At this condition:

$$\psi_{qr} = 0 \text{ and } \psi_{dr} = \psi_r = L_m i_{ds} \quad (5)$$

Let the two control parameters u_1 and u_2 define as given below that can simply the equation

$$u_1 = -\frac{R_s}{\sigma L_s} \text{ and } u_2 = \frac{R_r}{L_r} L_m \quad (6)$$

Therefore the eqns. (5) become

$$\frac{d}{dt} i_{ds} = u_1 i_{ds} + u_2 \frac{i_{qs}^2}{\psi_{dr}} + \omega_r i_{qs} + \frac{v_{ds}}{\sigma L_s} \quad (7)$$

$$\frac{d}{dt} i_{qs} = u_1 i_{qs} - u_2 \frac{i_{qs}}{\sigma L_m} - \frac{\omega_r}{\sigma} i_{ds} + \frac{v_{qs}}{\sigma L_s} \quad (8)$$

As from equation (6) that the rotor and stator resistances estimated by the control parameters u_1 and u_2 . After estimation the resistances are compensated by the controller.

3. Proposed Sliding Mode Controller Design

The controller is design to finds the control parameters u_1 and u_2 in such a way that the error arises between an actual and estimated values of d-axis and q-axis stator currents will be zero. The estimated currents are obtained from eqns. (7) and (8) as given below.

$$\dot{\hat{i}}_{ds} = \hat{u}_1 \hat{i}_{ds} + \hat{u}_2 \frac{\hat{i}_{qs}^2}{\psi_{dr}} + \omega_r \hat{i}_{qs} + \frac{v_{sd}}{\sigma L_s} \quad (9)$$

$$\dot{\hat{i}}_{qs} = \hat{u}_1 \hat{i}_{qs} - \hat{u}_2 \frac{\hat{i}_{qs}}{\sigma L_m} - \frac{\omega_r}{\sigma} \hat{i}_{ds} + \frac{v_{sd}}{\sigma L_s} \quad (10)$$

The sliding mode controller operated in such a way that the error “ e ” as well as its rate of change of \dot{e} move towards a sliding surface. Sliding surface can be obtained by the use of lyapunov stability theory.

Lyapunov stability theorem: It states that, if the projection of the system trajectories on sliding surfaces remains stable then the system is also stable. Thus the theorem can be formulated as:

Theorem: if a scalar function $V(x)$ is exist which is real, continuous and has continuous first partial derivatives with $V(x) > 0$ for $x \neq 0$; $V(0) = 0$

And its derivative $\dot{V}(x)$ is negative everywhere except the discontinuity surface then, the system is stable.

There is no specific method to find the Lyapunov function. However, V.I. Utkin[33] has discussed the method of using quadratic forms to find the sliding domain.

Generally, lyapunov function choose as $V = \frac{1}{2} e^T e$ where,

$$e = \begin{bmatrix} i_{ds} - \hat{i}_{ds} \\ i_{qs} - \hat{i}_{qs} \end{bmatrix} \quad (11)$$

$$\dot{V} = e^T \dot{e} = e^T \begin{bmatrix} \dot{i}_{ds} - \dot{\hat{i}}_{ds} \\ \dot{i}_{qs} - \dot{\hat{i}}_{qs} \end{bmatrix} \quad (12)$$

Substituting the values of actual and estimated stator currents from equations (7), (8), (9) and (10), in equation (12) for obtaining the expression of \dot{V}

$$\dot{V} = e^T \dot{e} = e^T A e + e^T B e_u \quad (13)$$

where,

$$\dot{e} = \begin{bmatrix} u_1 & \omega_r \\ -\frac{\omega_r}{\sigma} & u_1 \end{bmatrix} \begin{bmatrix} i_{ds} - \hat{i}_{ds} \\ i_{qs} - \hat{i}_{qs} \end{bmatrix} + \begin{bmatrix} \hat{i}_{ds} & \frac{i_{qs}^2}{\psi_{dr}^*} \\ \hat{i}_{qs} & \frac{i_{qs}}{\sigma L_m} \end{bmatrix} \begin{bmatrix} u_1 - \hat{u}_1 \\ u_2 - \hat{u}_2 \end{bmatrix} \quad (14)$$

$$A = \begin{bmatrix} u_1 & \omega_r \\ -\frac{\omega_r}{\sigma} & u_1 \end{bmatrix}, B = \begin{bmatrix} \hat{i}_{ds} & \frac{i_{qs}^2}{\psi_{dr}^*} \\ \hat{i}_{qs} & \frac{i_{qs}}{\sigma L_m} \end{bmatrix}, e_u = \begin{bmatrix} u_1 - \hat{u}_1 \\ u_2 - \hat{u}_2 \end{bmatrix}$$

$$\text{Let us assume that } \begin{bmatrix} i_{ds} - \hat{i}_{ds} \\ i_{qs} - \hat{i}_{qs} \end{bmatrix} = \begin{bmatrix} e i_{ds} \\ e i_{qs} \end{bmatrix}$$

As per the Lyapunov stability theorem, \dot{V} is negative everywhere for the stability of the system. The first term in equation (14) is negative as the A matrix is negative definite and the second term prove to be negative, which is given by

$$e^T B e_u = [e i_{ds} \quad e i_{qs}] \begin{bmatrix} \hat{i}_{ds} & \frac{i_{qs}^2}{\psi_{dr}^*} \\ \hat{i}_{qs} & \frac{i_{qs}}{\sigma L_m} \end{bmatrix} \begin{bmatrix} u_1 - \hat{u}_1 \\ u_2 - \hat{u}_2 \end{bmatrix} \quad (15)$$

The problem of tracking is similar to the remaining sliding surface for all time, and sliding variable is kept zero. We choose the sliding surfaces such that $e^T B e_u = 0$.

Switching surface is a line in second order system. Control input is applied to drive the system state over the switching line, and at once the system is constrained to remain on the line. For deciding the control input, two parameters are used i.e. the distance of an error trajectory from the sliding surface and also its rate of convergence. The sign of the control input must change where the

tracking error trajectory intersect with the sliding surface. In this way, the error trajectory is enforced to always move towards the sliding surface. Once it arrives at the sliding surface then, the system is constrained to slide along this surface to the equilibrium point. For estimation of u_1 and u_2 the sliding surface S_1 and S_2 is selected as given below respectively.

$$s = \begin{bmatrix} S_1 \\ S_2 \end{bmatrix} = \begin{bmatrix} e i_{ds} \hat{i}_{ds} + e i_{qs} \hat{i}_{qs} \\ e i_{ds} \frac{i_{qs}^2}{\psi_{dr}^*} - e i_{qs} \frac{i_{qs}}{\sigma L_m} \end{bmatrix} \quad (16)$$

The main drawback of the sliding mode controller (SMC) in real time application is the chattering problem to remove or reduce the chattering in the control, the order of the controller must be greater than one. In the proposed algorithm a Quasi second order SMC is choose because it provides the continuous control everywhere except the manifold, as a result the chattering effect reduces.

A Quasi second order SMC, provides the full SISO control based on the input measurement only. The homogeneous differentiator can be defined as [34].

$$\dot{z}_o = -\lambda_\delta L^{1/\delta} |z_o - s|^{((\delta-1)/\delta)} \text{sign}(z_o - s) + z_1 \quad (17)$$

$$\dot{z}_{\delta-1} = -\lambda_1 L \text{sign}(z_{\delta-1} - \dot{z}_o) \quad (18)$$

where δ is the order of the system. As from equation (4) the order of the system is second; $\delta = 2$ means the first derivative of the s is need.

As
 $\delta = 2$,

$$\dot{z}_o = -\lambda_2 L^{1/2} |z_o - s|^{(1/2)} \text{sign}(z_o - s) + z_1 \quad (19)$$

$$\dot{z}_1 = -\lambda_1 L \text{sign}(z_1 - \dot{z}_o)$$

Where $\lambda_2 L^{1/2}$ and $\lambda_1 L$ are positive constant and $\dot{s} = z_1$. The differentiator in equation (19) is used to derived the second order sliding homogeneous control signals is obtained as

$$\dot{\hat{u}} = \frac{-\alpha (\dot{s} + |s|^{1/2} \text{sign}(s))}{(|\dot{s} + |s|^{1/2}|)} \quad (20)$$

Where α is a positive constant.

By integrating the equation (20) we get the estimated values of the control parameter and indirectly the stator and rotor resistances.

The proposed algorithm is uncertain with the parametric variations of the system and due to the higher order, high frequency noise is also reduces. The block diagram of the proposed algorithm is shown in figure 1.

4. Simulation and Result

The Matlab/Simulink, is used to simulated the proposed controller. The simulation model and the results are presents in this section. Table 1 specified the machine parameters which are used in the simulation. The figure 2 shows the overall simulink model of the proposed controller with induction motor. There are four subsystems in this model

out of which one is the vector control block, the interior of this subsystem is shown in figure 3 from this simulink block generated the control pulse for the inverter. The second one is the subsystem1 shown in figure 4 from this the sliding surface for the sliding mode controller is generated, according to this sliding surface the two control signal u_1 and u_2 by using equation (20) form, the simulink block of this is shown in figure 5. These control signals signifies the estimated values of stator and rotor resistance as shown by the equation (6). The other subsystem in the main simulink model is the subsystem3 that represent the control unit of

the proposed system. The interior of the subsystem3 is representing in figure 6.

Table 1. Induction motor parameters

| Parameter | Notation | Value |
|-------------------|----------|--------------------------|
| Rotor resistance | R_r | 4.3047 Ω |
| Stator resistance | R_s | 6.65 Ω |
| Mutual inductance | L_m | 0.4475 H |
| Stator inductance | L_s | 0.4718 H |
| Rotor inductance | L_r | 0.4718 H |
| Rotor inertia | J | 0.0293 kg/m ² |
| Pole pair | p | 2 |

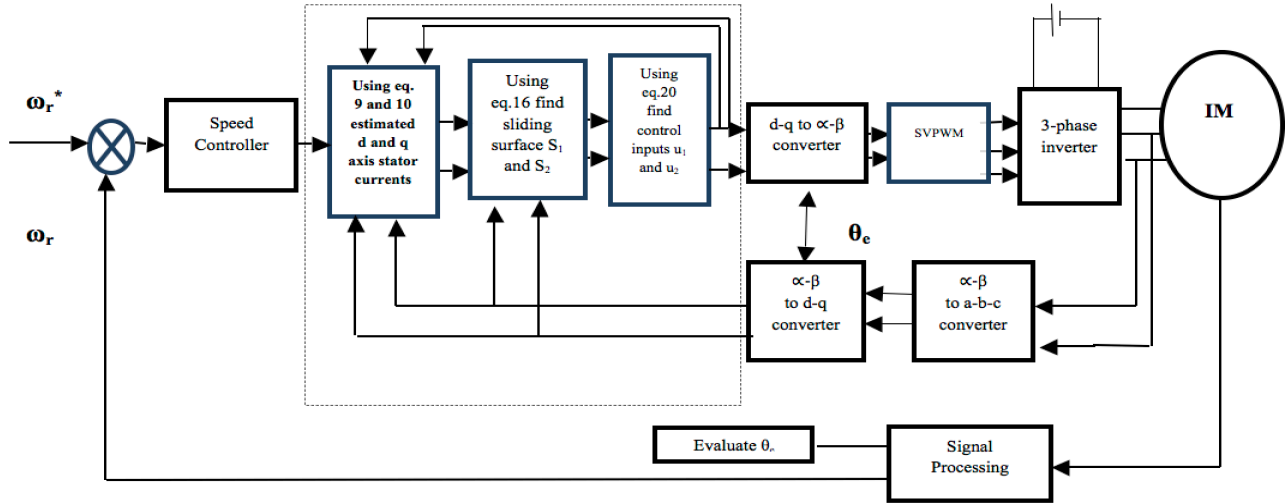


Fig.1 Block Diagram with Proposed Algorithm

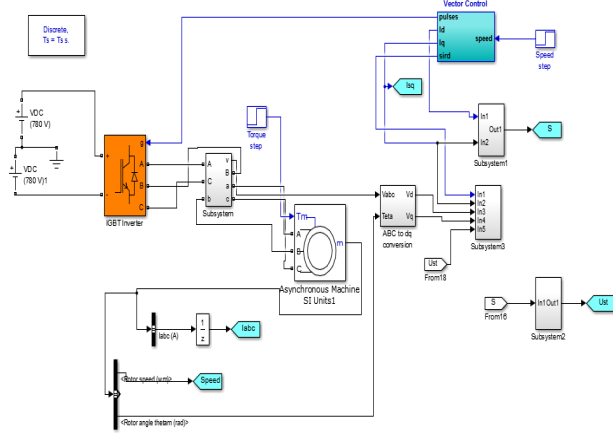


Fig. 2. Simulation Model of Induction motor with proposed controller

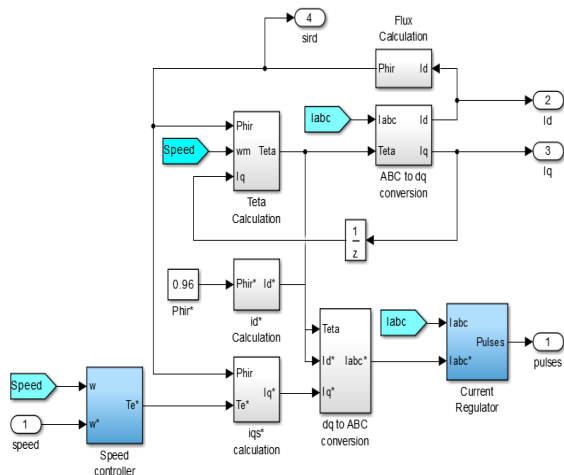


Fig. 3. Subsystem of Vector control

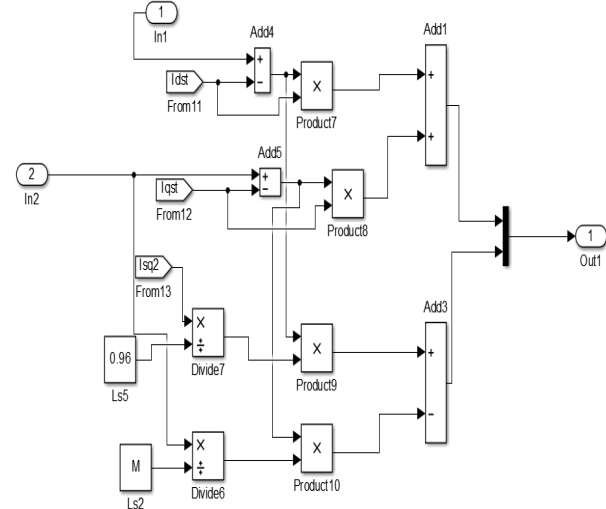


Fig. 4. Subsystem1 of sliding surface S

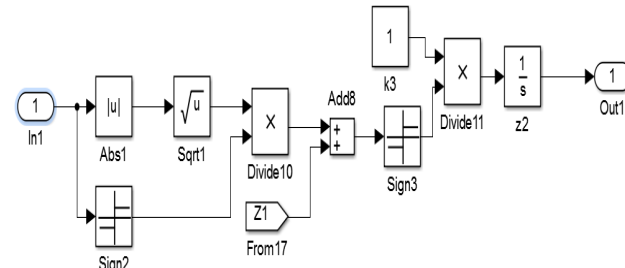


Fig. 5. Subsystem2 for control parameter u_1 and u_2

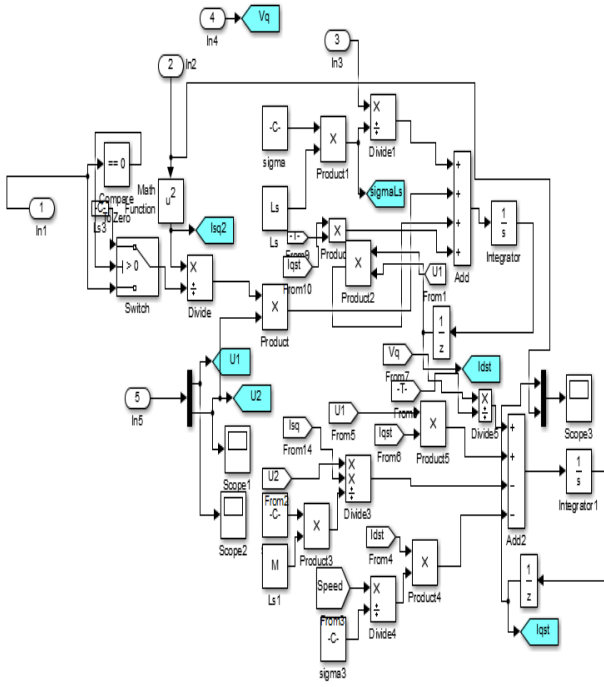


Fig. 6. Subsystem3 control block

The induction motor is run under a constant speed of let it be 30 rad/s and after a 2 sec. a load torque of 2 Nm is applied during this time the flux is established and attain a constant value in the machine. As observed from figure 7 and 8 the sliding surface S_1 and S_2 are reached then they are maintained even the parameters of the machines changed. By using estimated values of the control signal u_1 and u_2 as shown in figure 9 and 10 respectively, the values of stator and rotor resistances is calculated. As the estimated resistance values reach the actual on the sliding surfaces are reached they are maintained their irrespective of parameter variation. The estimated and actual values of the stator d and q axis currents showed in figure 11,12,13 and 14. The sliding surface not altered after reached, that certify the proposed method for compensation and estimation of machine parameters.

As seen from figure 7 and 8 the sliding surface are reached within 0.05 seconds means within a fraction of seconds the proposed algorithm estimate and compensate the rotor and stator resistance to their actual one where as the optimization techniques take a lot time and not give the accurate results. Even the Practical swarm optimization using online adaptation not give the quit accurate results in the fraction of time.

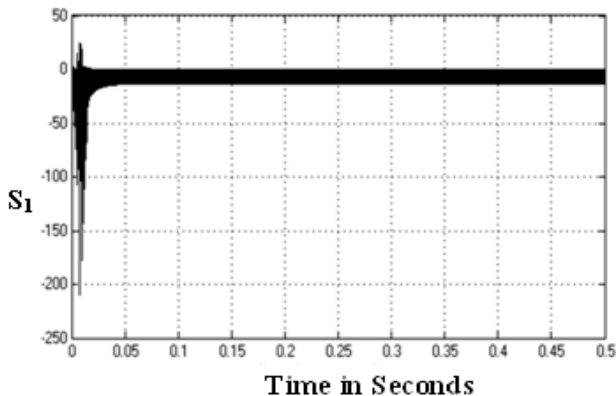


Fig. 7. The Sliding Surface S_1

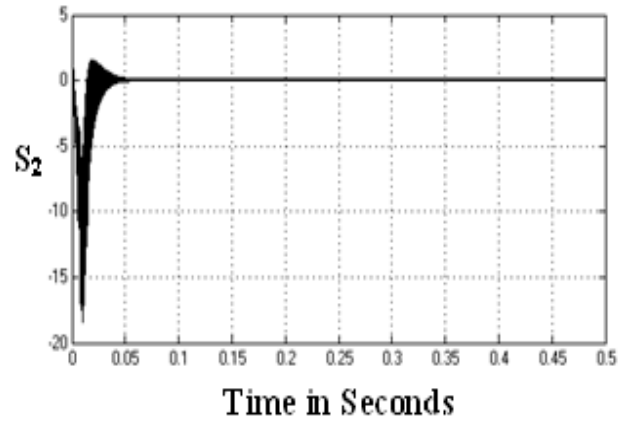


Fig. 8. The Sliding Surface S_2

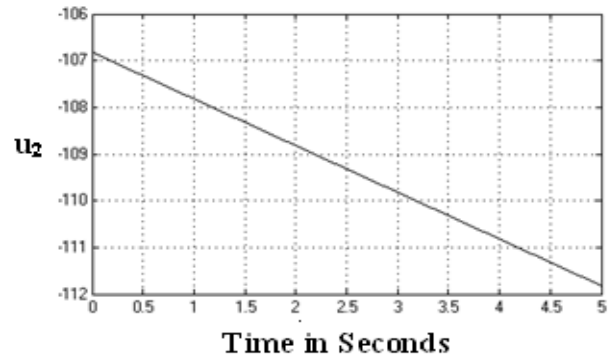


Fig. 9. Estimated value of u_2

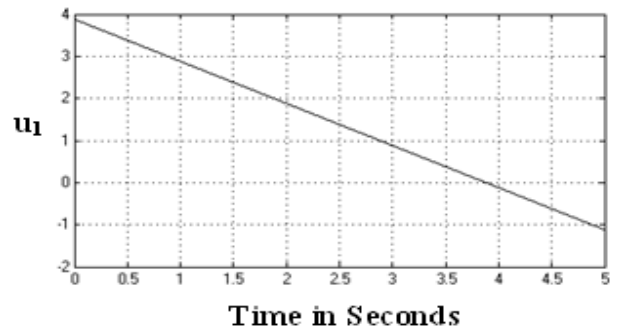


Fig. 10. Estimated value of u_1

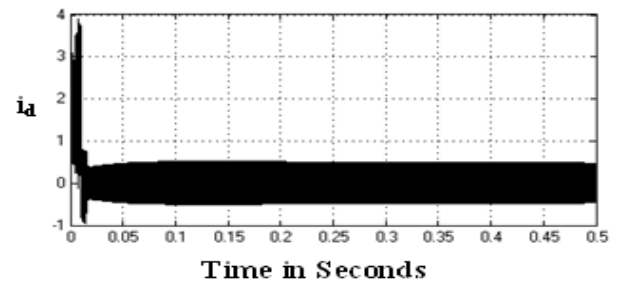


Fig. 11. Actual d-axis stator current

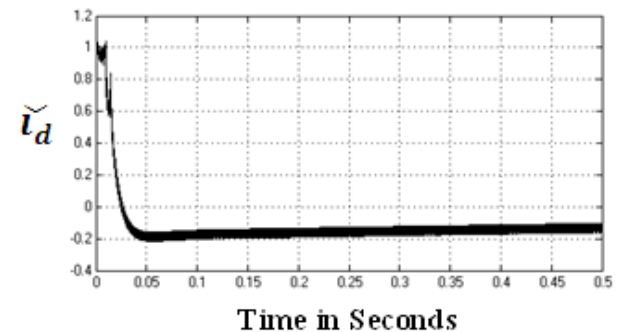


Fig. 12. Estimated value of d-axis current

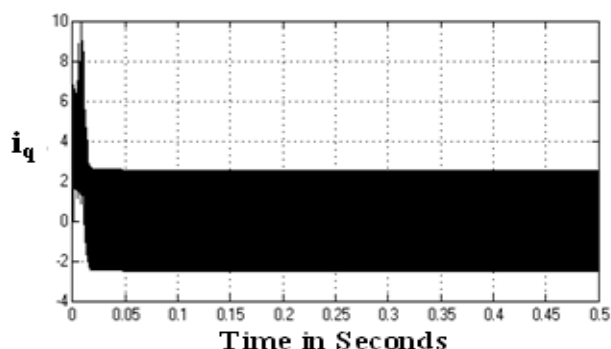


Fig. 13. Actual q-axis stator current

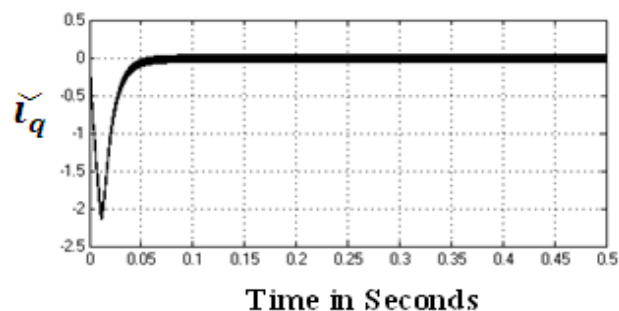


Fig. 14. Estimated value of q-axis current

5. Conclusion

A new algorithm using sliding mode control technique for induction motor parameters rotor and stator resistance estimation and compensation is proposed in this paper. The simulation done in Matlab/Simulink, the result shows the effectiveness of the proposed method. The proposed algorithm provides high dynamic response as the result analysis the system reach the sliding surface within 0.1 second and maintain their even the variation in resistances this shows the robustness of the method and the control signals u_1 and u_2 estimate as well as compensate R_1 and R_2 within 5 seconds that makes it better than other method of parameter compensation in induction motor. In the proposed algorithm assumed that the inductance is constant even the inductance also vary when the motor operates, in future the estimation and compensation of inductance also included in the proposed algorithm.

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